transfer effect smoothens the profiles. Finite kinetics may this produce the disappearance of instabilities but is not their cause.

The latter point may be the reason of the confusion in Zwiebel's paper: By varying the kinetics, the authors obtain profiles where the instabilities are present or absent. It then becomes tempting to interpret and explain them by kinetics only.

As a result, some of the conclusions drawn by Zwiebel are questionable. To mention but the most important (summary, line 11).

"The maojr significance of these instabilities is to elongate the depletion curves . . . (implying) . . . added effort during regeneration."

We believe this is not exact, or at least requires some qualification. If it were true, this would mean, for example, that, in Zwiebel's experiments, a 50/50 mixture of  $CO_2$  and  $C_2H_6$  would be more difficult to desorb than pure  $C_2H_6$ , (because there is an instability in the desorption of the mixture), whereas  $CO_2$  alone is more easily desorbed than  $C_2H_6$ .

Actually, in the desorption of a binary mixture, the non-key is desorbed preferentially, in a first front, where the desorption of the key is relatively retarded. After the desorption of the non-key is completed, the desorption of the key proceeds practically as if it had been present alone from the beginning, and the overall process does not require more regenerant.

Zwiebel's experimental results (his Figure 1) show this very clearly: the low end of the depletion curves of the key component does not depend on the concentration of the nonkey, even though the upper end does.

We should like to conclude by mentioning that multicomponent sorption has been abundantly studied by the equilibrium theory, and Glueckauf (1946, 1949, 1955) has shown and explained the existence of intermediate plateaus in binary profiles analogous to that of Zwiebel. This theory has now been widely generalized (Klein et al., 1967; Guiochon and Jacob, 1970; Rhee et al., 1970) and most of it published in book form (Aris and Amundson, 1973; Helfferich and Klein, 1970), but Zwiebel et al. seem unaware of this literature.

## NOTATION

$$X = \frac{\frac{dw_i/dc_i}{N K_{1,\text{key}}} = \frac{T}{\frac{v(1 + \alpha_{\text{nkey}} + \alpha_{\text{key}})}{\text{(a dimensionless time variable)}}$$

 $y = w_i/N$  (a dimensionless concentration variable)

N = saturation value of the adsorbent

i = designates key or nonkey component

w, c, v,  $\alpha$ , T, K are defined in Zwiebel's paper

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D. Tondeur and M. Bailley CNRS Lab des Sciences du Génie Chimique 54042 Nancy CEDEX France

## TO THE EDITOR:

It seems that your correspondents, D. Tondeur and M. Bailly, have misunderstood the paper in question [AIChE J., 20, 915 (1974)]. They claim that we have studied various kinetic criteria to obtain the results and that we sought the existence of the indicated instabilities within these kinetic models. On the contrary, while we solved a more-or-less realistic model which includes a kinetic element, our objective was to study "the effects of concentration variations, component interactions and equilibrium characteristics." This, in terms of the corre-

spondents' language is equivalent to "competitive coupling of the sorption of the components."

To emphasize our appreciation of the importance of the coupling effects, we arbitrarily picked a single kinetic condition, that is, the case where the rate coefficients of the two adsorbing species are identical,  $\phi_i = 1$ , and kept it constant for the entire analysis. Finally, we reported the location of the instabilities in terms of  $\alpha_{NK}^{\bullet}$  and  $\eta$  (Figure 12), both parameters related only to the prevailing equilibrium and capacity conditions.

Indeed, your correspondents are correct to point out that the kinetics have " no bearing upon the existence of the instabilities. In fact, they show that an equilibrium (infinite rate) would also predict such instabilities. However, please note that the usual practice in such equilibrium model analyses is to differentiate with respect to time the isotherm equation and use the resulting expression in the gas phase mass balance for the rate of interface mass transfer. If such differentiation is carried out on the Langmuir equation written for binary mixtures, two terms result which closely resemble the driving force expression of the film model rate equation. In other words, the equilibrium model is reduced to an analysis, as was originally stipulated with the film model, involving the difference between two terms. Our intent in incorporating a kinetic condition in the model is based upon our desire to simulate real systems. Our experience indicates that there are very few adsorption systems that are equilibrium controlled, especially in the case of multicomponent systems.

IMRE ZWIEBEL WORCESTER POLYTECHNIC INSTITUTE WORCESTER, MASSACHUSETTS 01609

## **ERRATUM**

The paper "A Generalized Thermodynamic Correlation Based on Three-Parameter Corresponding States" by B. I. Lee and M. G. Kesler, *Journal*, 21, 510 (1975) has an error in Eq. (15). It should read:

$$\left(\frac{P_r}{T_r}\right)_{V_r} = \frac{1}{V_r} \left\{ \dots + \frac{c_1 - 2c_3/T_r^3}{V_r^2} + \frac{d_1}{V_r^5} \right\}$$